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XII MATHEMATICS

HOLIDAY HOMEWORK(TO BE DONE ON PRACTISE NOTEBOOK)

- Let R be a relation on the set N be defined by $\{(x, y) \mid \forall x, y \in N, 2x + y = 41\}$. Then, R is
 - Reflexive
 - Symmetric
 - Transitive
 - None of these
 - For real numbers x and y , we write $x R y \leftrightarrow x - y + \sqrt{2}$ is an irrational number. Then, the relation R is
 - Reflexive
 - Symmetric
 - Transitive
 - None of these
 - The relation $R = \{(1, 1), (2, 2), (3, 3), (1, 2), (2, 3), (1, 3)\}$ on set $A = \{1, 2, 3\}$ is
 - Reflexive but not symmetric
 - Reflexive but not transitive
 - Symmetric and transitive
 - Neither symmetric nor transitive
 - Consider the non-empty set consisting of children in a family and a relation R defined as $a R b$ if a is brother of b . Then R is
 - symmetric but not transitive
 - transitive but not symmetric
 - neither symmetric nor transitive
 - both symmetric and transitive
 - Let $P = \{(x, y) : x^2 + y^2 = 1, x, y \in R\}$. Then, P is
 - Reflexive
 - Symmetric
 - Transitive
 - Anti-symmetric
- Let S be the set of all real numbers. Then, the relation $R = \{(a, b) : 1 + ab > 0\}$ on S is
 - Reflexive and symmetric but not transitive
 - Reflexive and transitive but not symmetric
 - Symmetric, transitive but not reflexive
 - Reflexive, transitive and symmetric
 - Let R be the relation in the set Z of all integers defined by $R = \{(x, y) : x - y \text{ is an integer}\}$. Then R is
 - reflexive
 - symmetric
 - transitive
 - an equivalence relation
- For the set $A = \{1, 2, 3\}$, define a relation R in the set A as follows $R = \{(1, 1), (2, 2), (3, 3), (1, 3)\}$ Then, the ordered pair to be added to R to make it the smallest equivalence relation is
 - $(1, 3)$
 - $(3, 1)$
 - $(2, 1)$
 - $(1, 2)$

11. Let $A = \{1, 2, 3\}$ and $R = \{(1, 2), (2, 3)\}$ be a relation in A . Then, the minimum number of ordered pairs may be added, so that R becomes an equivalence relation, is
 a. (a) 7 (b) 5 (c) 1 (d) 4
12. Let $A = \{1, 2, 3\}$. Then, the number of relations containing $(1, 2)$ and $(1, 3)$, which are reflexive and symmetric but not transitive, is
 a. (a) 1 (b) 2 (c) 3 (d) 4
13. Let $f : \mathbb{R} \rightarrow \mathbb{R}$ be a function defined by $f(x) = x^3 + 4$, then f is
 a. (a) Injective (b) Surjective (c) Bijective (d) None of these
14. Let $X = \{0, 1, 2, 3\}$ and $Y = \{-1, 0, 1, 4, 9\}$ and a function $f : X \rightarrow Y$ defined by $y = x^2$, is
 15. one-one onto (b) one-one into (c) many-one onto (d) many-one into
16. Let $g : \mathbb{R} \rightarrow \mathbb{R}$ $g(x) = x^2 - 4x - 5$, then
 17. g is one-one on \mathbb{R} (b) g is not one-one on \mathbb{R}
 18. g is bijective on \mathbb{R} (d) None of these
19. The mapping $f : \mathbb{N} \rightarrow \mathbb{N}$ given by $f(n) = 1 + n^2$, $n \in \mathbb{N}$ when \mathbb{N} is the set of natural numbers, is
20. The function $f : \mathbb{R} \rightarrow \mathbb{R}$ given by $f(x) = x^3 - 1$ is
 a. (a) a one-one function (b) an onto function
 b. (c) a bijection (d) neither one-one nor onto
21. A function $f : X \rightarrow Y$ is said to be onto, if for every $y \in Y$, there exists an element x in X such that
 a. (a) $f(x) = y$ (b) $f(y) = x$ (c) $f(x) + y = 0$ (d) $f(y) + x = 0$
22. Let R be the relation in the set $\{1, 2, 3, 4\}$ given by $R = \{(1, 2), (2, 2), (1, 1), (4, 4), (1, 3), (3, 3), (3, 2)\}$.
 (a) R is reflexive and symmetric but not transitive
 (b) R is reflexive and transitive but not symmetric
 (c) R is symmetric and transitive but not
 (d) R is equivalence relation
23. Let $A = \{1, 2, 3\}$ and $B = \{a, b, c\}$, then the number of bijective functions from A to B are
 a. (a) 2 (b) 8 (c) 6 (d) 4
24. The number of surjective functions from A to B where $A = \{1, 2, 3, 4\}$ and $B = \{a, b\}$ is
 a. (a) 14 (b) 12 (c) 2 (d) 15

25. The function $f : \mathbb{R} \rightarrow \mathbb{R}$ defined by $f(x) = (x - 1)(x - 2)(x - 3)$ is
- a. (a) one-one but not onto (b) onto but not one-one
 26. (c) both one-one and onto (d) neither one-one nor onto
27. If $\begin{bmatrix} 2 & 1 \\ 3 & 2 \end{bmatrix} A \begin{bmatrix} -3 & 2 \\ 5 & -3 \end{bmatrix} = I_2$, then $A =$
- a. (a) $\begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$ (b) $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$ (c) $\begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$ (d) $\begin{bmatrix} 0 & 1 \\ 1 & 1 \end{bmatrix}$
28. If $A = \begin{bmatrix} 3 & 2 \\ 0 & 1 \end{bmatrix}$, then $(A^{-1})^3$ is equal to
- a. (a) $\frac{1}{27} \begin{bmatrix} 1 & -26 \\ 0 & 27 \end{bmatrix}$ (b) $\frac{1}{27} \begin{bmatrix} 1 & 26 \\ 0 & 27 \end{bmatrix}$ (c) $\frac{1}{27} \begin{bmatrix} 1 & -26 \\ 0 & -27 \end{bmatrix}$
 (d) $\frac{1}{27} \begin{bmatrix} -1 & -26 \\ 0 & -27 \end{bmatrix}$
29. If $A = \begin{bmatrix} 0 & 3 \\ 2 & 0 \end{bmatrix}$ and $A^{-1} = mA$, then m is equal to
- a. (a) $-1/6$ (b) $1/3$ (c) $-1/3$ (d) $1/6$
30. If I_3 is the identity matrix of order 3, then $I_3^{-1} =$
- a. (a) O (b) $3I_3$ (c) I_3 (d) Not necessarily exist
31. If A and B are 2 non-zero matrices such that $AB = 0$, then
- (a) both A and B are singular (b) either of them is singular
 (c) neither of them is singular (d) none of these
32. If A is a singular matrix then $\mathbf{A.adjA} =$
- (a) is a scalar matrix (b) is a zero matrix
 (c) is an identity matrix (d) none of these
33. For how many integral values of x in the closed interval $[-4, -1]$, matrix
- $$\begin{bmatrix} 3 & -x-1 & 2 \\ 3 & -1 & x+2 \\ x+3 & -1 & 2 \end{bmatrix}$$
- is singular?
- (a) Zero (b) 2 (c) 1 (d) 3
34. If A and B are square matrices of size $n \times n$, such that $A^2 - B^2 = (A+B)(A-B)$, then which one of the following is always true-
- (a) $AB = BA$ (b) either of A or B is a zero matrix
 (c) Either of A or B is an identity matrix (d) $A = B$
35. If $[a_{ij}]_{n \times n}$ be a diagonal matrix with diagonal element all different and $B = [b_{ij}]_{n \times n}$ be some matrix. Let $AB = [c_{ij}]_{n \times n}$, then c_{ij} is equal to
- a) $a_{jj}b_{ij}$ (b) $a_{ii}b_{ij}$ (c) $a_{ij}b_{ij}$ (d) $a_{ij}b_{ji}$
36. If A is a skew matrix of odd order, then $|\text{adj}A|$ is equal to

- (a) 0 (b) n (c) n^2 (d) none of these
37. A square matrix P satisfies $P^2 = I - P$ where I is the identity matrix. If $P^n = 5I - 8P$, then $n =$
 (a) 4 (b) 5 (c) 6 (d) 7
38. If $A = \begin{bmatrix} 4 & x+2 \\ 2x-3 & x+1 \end{bmatrix}$ is symmetric, then $x =$
 (a) 3 (b) 5 (c) 2 (d) 4
39. If A is 3×4 matrix and B is a matrix such that $A'B$ and BA' are defined, then B is of the type
 (a) 3×4 (b) 3×3 (c) 4×4 (d) 4×3

CASE STUDY QUESTIONS

1. Aman and Ramesh are playing Ludo at home during Covid-19. While rolling the dice, Aman's sister Lata observed and noted the possible outcomes of the throw every time belongs to set $\{1, 2, 3, 4, 5, 6\}$. Let A be the set of players while B be the set of all possible outcomes. Let $A = \{A, R\}$, $B = \{1, 2, 3, 4, 5, 6\}$. Using the information given above, answer the following:
- (i) Let $R: B \rightarrow B$ be defined by $R = \{(x, y) : y = x\}$ is
 (a) Reflexive and transitive but not symmetric
 (b) Reflexive and symmetric but not transitive
 (c) Reflexive but not symmetric and transitive
 (d) Equivalence
- (ii) Let $R: B \rightarrow B$ be defined by $R = \{(1, 2)(2, 2)(1, 3)(3, 4)(3, 1)(4, 3)(5, 5)\}$. Then R is
 (a) Symmetric (b) Reflexive
 (c) Transitive (d) None of these three
- (iii) Let $R: B \rightarrow B$ be defined by $R = \{(2, 1)(1, 2)(2, 2)(3, 3)(4, 4)(5, 5)(6, 6)\}$, then R is
 (a) Symmetric (b) Reflexive and Transitive (c) Transitive and symmetric (d) Equivalence
- (iv) Lata wants to know the number of relations possible from A to B . How many relations are possible?
 (a) 36 (b) 64 (c) $6!$ (d) 2^{12}

(v) Lata wants to know the number of functions from $A \rightarrow B$, How many numbers of functions are possible?

(a) 36

(b) 64

(c) 6!

(d) 2^{12}

2. A Robot works on the software which follows function $f(x) = \frac{x-2}{x-1}$. If the value of domain is put in place of x . This robot works and performs various works. Based on the above information, answer the following:

(i) What will the value/values of x , on which this robot works

(a) On all real values

(b) On all real values except 1

(c) On all real values except 2

(d) On all real values except $\{1, 2\}$

(ii) If range denotes the number of works performed, then range of the works performed will be

(a) $R - \{1\}$

(b) $R - \{2\}$

(c) $R - \{1, 2\}$

(d) On all real values

(iii) If this function is defined from $f: R - \{1\} \rightarrow R - \{1\}$

(a) Injective

(b) Surjective

(c) Bijective

(d) Into

(iv) If a Robot follows the $f: R - \{1\} \rightarrow R$, then $f(x)$ is

(a) Injective

(b) Surjective

(c) Bijective

(d) Into

(v) If a Robot follows the $f: N - \{1\} \rightarrow R - \{1\}$, then $f(x)$ is

(a) Injective

(b) Surjective

(c) Bijective

(d) Into

Revise chapter No. 1, 2, 3 from Ncert textbook and exemplar.